

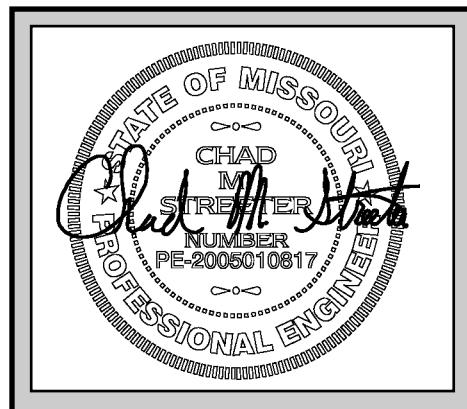
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Lots 152, 153 & 154  
Lee's Summit, Missouri

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**Reinforced Soil Retaining Wall Design**



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# Segmental Retaining Wall Design Calculations per NCMA

## Wall Geometry

Height $H := 11.0 \cdot \text{ft}$	Backslope $\beta := 10.0 \cdot \text{deg}$	Dead Load $q_d := 0 \cdot \text{psf}$	Live Load $q_l := 0 \cdot \text{psf}$	Distance to Slope $Z := 1.0 \cdot \text{ft}$	Wall below grade at toe $H_{cmb} := .67 \cdot \text{ft}$
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## Soil Properties

Reinforced Soil (Internal)	Retained Soil (External)	Drainage Fill	Foundation Soil	Pullout
$\gamma_i := 110 \cdot \text{pcf}$	$\gamma_e := 120 \cdot \text{pcf}$	$\gamma_d := 110 \cdot \text{pcf}$	$\gamma_f := 120 \cdot \text{pcf}$	$C_i := 0.7$
$\phi_i := 32 \cdot \text{deg}$	$\phi_e := 26 \cdot \text{deg}$	$\phi_d := 32 \cdot \text{deg}$	$\phi_f := 26 \cdot \text{deg}$	
$C_{dsi} := 0.8$	$C_{dse} := 1.0$		$c_f := 0.0 \text{ psf}$	

## Segmental Unit Properties

Height $H_u := 8 \cdot \text{in}$	Length $L_u := 18 \cdot \text{in}$	Width $W_u := 12 \cdot \text{in}$	Setback $\Delta_u := 1.0 \cdot \text{in}$	Center of Gravity $G_u := 6 \cdot \text{in}$	Batter $\omega := \tan\left(\frac{\Delta_u}{H_u}\right)$ $\omega = 7.125 \cdot \text{deg}$
Infilled Unit Weight $\gamma_u := 120 \cdot \text{pcf}$		Hinge Height $H_h := \text{if} \left[ \tan(\omega) = 0, H, \left[ 2 \cdot \frac{(W_u - G_u)}{\tan(\omega)} \right] \right] \Rightarrow H_h = 8 \text{ ft}$			
					[Eq. 4-1]

### Internal Interface Friction Angle

$$\delta_i := \frac{2}{3} \cdot \phi_i \quad [\delta_i = 21.33 \cdot \text{deg}] \quad [\text{Eq. 3-17}]$$

### Internal Active Earth Pressure

$$K_{ai} := \frac{\cos(\phi_i + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_i) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_i + \delta_i) \cdot \sin(\phi_i - \beta)}{\cos(\omega - \delta_i) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{ai} = 0.256]$$

### External Interface Friction Angle

$$\delta_e := \text{if}(\phi_i > \phi_e, \phi_e, \phi_i) \quad [\delta_e = 26 \cdot \text{deg}] \quad [\text{Eq. 3-16}]$$

### External Active Earth Pressure

$$K_{ae} := \frac{\cos(\phi_e + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_e) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_e + \delta_e) \cdot \sin((\phi_e - \beta))}{\cos(\omega - \delta_e) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{ae} = 0.339]$$

### Orientation of Critical Internal Failure Surface

$$\alpha_i := \text{atan} \left[ \frac{-\tan(\phi_i - \beta) + \sqrt{(\tan(\phi_i - \beta)) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega)) \cdot (1 + \tan(\delta_i - \omega) \cdot \cot(\phi_i + \omega))}}{1 + \tan(\delta_i - \omega) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega))} \right] + \phi_i \quad [\text{Eq. 3-14}] \quad [\alpha_i = 52.419 \cdot \text{deg}]$$

### Orientation of Critical External Failure Surface

$$\alpha_e := \text{atan} \left[ \frac{-\tan(\phi_e - \beta) + \sqrt{\tan(\phi_e - \beta) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega)) \cdot (1 + \tan(\delta_e - \omega) \cdot \cot(\phi_e + \omega))}}{1 + \tan(\delta_e - \omega) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega))} \right] + \phi_e \quad [\text{Eq. 3-14}] \quad [\alpha_e = 46.452 \cdot \text{deg}]$$

**Sliding****External Stability Analysis**

Given

$$\min \left[ \frac{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_e)}{1.5} \cdot \tan(\phi_d) \right]$$

$$= \frac{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_f)}{1.5}$$

$$= \frac{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \dots + (q_d + q_l) \cdot K_a_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]}{1.5}$$

**Overspinning**

$L_{\text{sliding}} := \text{Find}(L)$

$L_{\text{sliding}} = 6.035 \text{ ft}$

Given

$$2.0 = \frac{\left[ (L \cdot \gamma_e \cdot H) \cdot \left[ \frac{1}{2} \cdot (L + H \cdot \tan(\omega)) \right] \right] \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \cdot \left[ H \cdot \tan(\omega) + W_u + Z + \frac{2}{3} \cdot (L - W_u - Z) \right] + q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \frac{Z + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right]}{2} + H \cdot \tan(\omega) +}{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{3} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{2} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]}$$

$L_{\text{overtur}} := \text{Find}(L)$

$L_{\text{overtur}} = 4.73 \text{ ft}$

$$L := \max \begin{pmatrix} L_{\text{sliding}} \\ L_{\text{overtur}} \\ 0.6 \cdot H \end{pmatrix}$$

$L = 6.6 \text{ ft}$

Based on Overspinning and Sliding:

$L := 8.0 \text{ ft}$

(Round up L)

## Eccentricity

$$L' := L - W_u - Z$$

$$L' = 6 \text{ ft}$$

[Fig. 2-10] [Eq. 5-1]

$$L'' := \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)}$$

$$L'' = 0.135 \text{ ft}$$

[Fig. 2-10] [Eq. 5-2]

$$L_\beta := L' + L''$$

$$L_\beta = 6.135 \text{ ft}$$

[Fig. 2-10] [Eq. 5-3]

$$h := L_\beta \cdot \tan(\beta)$$

$$h = 1.082 \text{ ft}$$

[Fig. 2-10] [Eq. 5-4]

$$W_{ri} := L \cdot \gamma_i \cdot H$$

$$W_{ri} = 9680 \cdot \text{plf}$$

[Eq. 5-15]

$$X_{ri} := \frac{1}{2} \cdot (L + H \cdot \tan(\omega))$$

$$X_{ri} = 4.688 \text{ ft}$$

[Eq. 5-19]

$$W_{r\beta} := \frac{1}{2} \cdot \gamma_i \cdot (L' - Z) \cdot h$$

$$W_{r\beta} = 297.497 \cdot \text{plf}$$

[Eq. 5-16]

$$X_{r\beta} := H \cdot \tan(\omega) + W_u + \frac{2}{3} \cdot L_\beta + Z$$

$$X_{r\beta} = 7.465 \text{ ft}$$

[Eq. 5-20]

$$X_{q\beta} := \frac{Z + L_\beta}{2} + [(H + h) \cdot \tan(\omega)] + W_u$$

$$X_{q\beta} = 6.078 \text{ ft}$$

[Eq. 5-21]

Actual Height of wall:

$$H_s := (H + h)$$

$$H_s = 12.082 \text{ ft}$$

Earth Pressures:

$$P_{sH} := \left[ \frac{1}{2} \cdot K_a e \cdot \gamma_e \cdot (H + h)^2 \cdot \cos(\delta_e - \omega) \right]$$

$$P_{sH} = 2809.743 \cdot \text{plf}$$

[Eq. 5-6]

$$Y_s := \frac{1}{3} \cdot (H + h)$$

$$Y_s = 4.027 \text{ ft}$$

[Eq. 5-9]

$$P_{qH} := (q_d + q_l) \cdot K_a e \cdot (H + h) \cdot \cos(\delta_e - \omega)$$

$$P_{qH} = 0 \cdot \text{plf}$$

[Eq. 5-8]

$$Y_q := \frac{1}{2} \cdot (H + h)$$

$$Y_q = 6.041 \text{ ft}$$

[Eq. 5-10]

$$\textcolor{brown}{e} := \frac{\left[ P_{sH} \cdot Y_s + P_{qH} \cdot Y_q - W_{ri} \cdot \left( X_{ri} - \frac{L}{2} \right) - W_{r\beta} \cdot \left( X_{r\beta} - \frac{L}{2} \right) - q_d \cdot (L_\beta) \cdot \left( X_{q\beta} - \frac{L}{2} \right) \right]}{W_{ri} + W_{r\beta} + q_d \cdot (L_\beta)}$$

$$e = 0.3638 \text{ ft}$$

[Eq. 5-25]

Check  $\textcolor{brown}{e} := \text{if}(e \leq 0, 0.075L, e)$

$$e = 0.364 \text{ ft}$$

Surcharge is applied over:  $(L' + L'') = 6.135 \text{ ft}$

$$B := L - 2 \cdot e$$

$$B = 7.272 \text{ ft}$$

[Eq. 5-24]

## Bearing Capacity

$$Q_a := \frac{[W_{ri} + W_{rf\beta} + (q_d + q_l) \cdot (L' + L'')]}{B}$$

$$Q_a = 1371.964 \cdot \text{psf}$$

$$N_q := \tan\left(45^\circ - \frac{\phi_f}{2}\right)^2 \cdot \exp(\pi \cdot \tan(\phi_f))$$

$$N_q = 11.854$$

[Fig. 4-5]

$$N_c := \text{if } [\phi_f = 0, 5.14, (N_q - 1) \cdot \cot(\phi_f)]$$

$$N_c = 22.254$$

[Fig. 4-5]

$$N_\gamma := 2 \cdot (N_q + 1) \cdot \tan(\phi_f)$$

$$N_\gamma = 12.539$$

[Fig. 4-5]

$$Q_{ult} := c_f \cdot N_c + \frac{1}{2} \cdot \gamma_f \cdot B \cdot N_\gamma + \gamma_f \cdot H_{emb} \cdot N_q$$

$$Q_{ult} = 6424.334 \cdot \text{psf}$$

[Eq. 4-20]

$$FS_{bearing} := \frac{Q_{ult}}{Q_a}$$

$$FS_{bearing} = 1$$

[Eq. 4-19]

## Internal Stability

### Reinforcement Properties

#### Geogrid Design Data

Backfill Soil      Type := (gravel)

1    2    3    4    5    6    7    8    9

Geogrid Number

$$\text{Type}^T = (411 \ 834 \ 1199 \ 1336 \ 2004 \ 2508 \ 3011 \ 3873 \ 7914)$$

$$GN1 := 4$$

$$GN2 := 2$$

$$\text{inter}^T = (1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 0)$$

$$\text{slope}^T = (38 \ 38 \ 38 \ 38 \ 38 \ 38 \ 0)$$

$$\text{maxc}^T = (4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 0) \quad x := 4..1 \quad x \text{ is the number of grids at the top of the wall of a different type}$$

$$T_a := \text{Type}_{GN1} \cdot \text{plf} \quad T_a = 1336 \cdot \text{plf}$$

$$T_{a2} := \text{Type}_{GN2} \cdot \text{plf} \quad T_{a2} = 834 \cdot \text{plf}$$

$$a_{cs} := \text{inter}_{GN1} \cdot \text{plf} \quad a_{cs} = 1145 \cdot \text{plf}$$

$$\lambda_{cs} := \text{slope}_{GN1} \cdot \text{deg} \quad \lambda_{cs} = 38 \cdot \text{deg}$$

$$V_{csmax} := \text{maxc}_{GN1} \cdot \text{plf} \quad V_{csmax} = 4540 \cdot \text{plf}$$

$$a_{cs2} := \text{inter}_{GN2} \cdot \text{plf} \quad a_{cs2} = 1145 \cdot \text{plf}$$

$$\lambda_{cs2} := \text{slope}_{GN2} \cdot \text{deg} \quad \lambda_{cs2} = 38 \cdot \text{deg}$$

$$V_{csmax2} := \text{maxc}_{GN2} \cdot \text{plf} \quad V_{csmax2} = 4540 \cdot \text{plf}$$

## Tension in Geogrid

Number of Grids:	Grig Spacing (ft):	# of grids for that spacing:	Depth of first grid (ft):	Length of grids:
$n_g := 4$	Spacing1 := 2	$n_1 := 4$	$h_1 := 3.67$	$L_1 := 8.0 \quad L_2 := 8.0 \quad L_t := \frac{L}{\text{ft}}$
	Spacing2 := 1.67	$n_2 := 0$		

Make all zero when using one geogrid

Note: make sure that the elevations don't exceed the height of the wall (H)  $H = 11 \text{ ft}$

$$\text{top} := \text{length}(E) \quad p := 2 \dots \text{top} \quad \text{top} = 4$$

$$\text{grids} := \text{length}(E) \quad n := 1 \dots \text{top} \quad l := 1 \dots \text{grids} - 1$$

$$E = \begin{pmatrix} 3.67 \\ 5.67 \\ 7.67 \\ 9.67 \end{pmatrix} \text{ ft}$$

$$T_{a_x} := T_{a2} \quad T_{a_x} = \begin{pmatrix} 834 \\ 834 \\ 834 \\ 834 \end{pmatrix} \cdot \text{plf} \quad T_a := \overrightarrow{\frac{L \cdot T_a}{L}}$$

$$T_a = \begin{pmatrix} 1336 \\ 1336 \\ 1336 \\ 1336 \end{pmatrix} \cdot \text{plf}$$

$$L = \begin{pmatrix} 8 \\ 8 \\ 8 \\ 8 \end{pmatrix} \text{ ft}$$

$$T_a^T = (834 \ 834 \ 834 \ 834) \cdot \text{plf}$$

$$D_p := \frac{E_{p-1} + E_p}{2} \quad D_1 := 0 \cdot \text{ft} \quad D_{\text{grids}+1} := H$$

$$D^T = (0 \ 4.67 \ 6.67 \ 8.67 \ 11) \text{ ft}$$

### Total Applied Tensile Strength in the Geosynthetic reinf.:

$$F_{g_n} := \int_{D_n}^{D_{(n+1)}} (\gamma_i \cdot D + q_l + q_d) \cdot K a_i \cdot \cos(\delta_i - \omega) \, dD \quad [\text{Eq. 5-36}]$$

$$F_g^T = (297.624 \ 309.512 \ 418.687 \ 625.453) \cdot \text{plf}$$

### Safety factor:

$$FS_{ten_n} := \frac{T_{a_n}}{F_{g_n}} \quad FS_{ten}^T = (2.802 \ 2.695 \ 1.992 \ 1.333)$$

## Pullout Capacity

### Anchorage Length of Geosynthetic

$$La_n := L_n - W_u - [(H + h) - E_n] \cdot \tan(90^\circ - \alpha_i) + [(H + h) - E_n] \cdot \tan(\omega) \quad [\text{Eq. 5-46}]$$

$$La^T = (1.578 \ 2.867 \ 4.156 \ 5.445) \text{ ft}$$

**Note:** If the anchorage length is less than 1ft then there is not enough embedment length and it has to be increased. Note that in some cases it might just be the top two grids.

### Average Depth of overburden on Anchorage length

$$d_n := E_n + \left[ (H - E_n) \cdot \tan(90^\circ - \alpha_i) + \frac{La_n}{2} - (Z + H \cdot \tan(\omega) - \Delta_u) \right] \cdot \tan(\beta) \quad [\text{Eq. 5-47}]$$

$$d^T = (4.4 \ 6.242 \ 8.084 \ 9.926) \text{ ft}$$

### Anchorage Capacity

$$AC_n := 2 \cdot La_n \cdot C_i \cdot (d_n \cdot \gamma_i + q_d) \cdot \tan(\phi_i) \quad [\text{Eq. 5-45}]$$

$$AC^T = (668.05 \ 1722.134 \ 3233.307 \ 5201.567) \text{ plf}$$

$$F_g^T = (297.624 \ 309.512 \ 418.687 \ 625.453) \text{ plf}$$

### Safety Factor

$$FS_{po} := \frac{\overrightarrow{AC}}{F_g} \quad [\text{Eq. 5-44}]$$

$$FS_{po}^T = (2.245 \ 5.564 \ 7.722 \ 8.316)$$

## Internal Sliding

### Reduced reinforcement length

$$\Delta L_{l+1} := \begin{cases} \left[ (E_{l+1} - E_l) \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) \right] & \text{if } n_g > 2 \\ \text{Spacing1} \cdot \text{ft} \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) & \text{if } n_g = 2 \\ 0 & \text{if } n_g = 1 \end{cases} \quad [\text{Eq. 5-51}]$$

$$\Delta L^T = (0 \ 1.651 \ 1.651 \ 1.651) \text{ ft}$$

$$L'_{s_n} := L_n - W_u - \Delta L_n \quad [\text{Eq. 5-50}]$$

$$L'_s^T = (7 \ 5.349 \ 5.349 \ 5.349) \text{ ft}$$

### Length of sloping ground

$$L_{s\beta_n} := L'_{s_n} + \frac{(L'_{s_n} - W_u) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} - Z \quad [\text{Eq. 5-53 & 5-52}]$$

$$\boxed{L_{s\beta}^T = (6.135 \ 4.447 \ 4.447 \ 4.447) \text{ ft}}$$

### Height of slope above crest of wall

$$h'_n := L_{s\beta_n} \cdot \tan(\beta) \quad [\text{Eq. 5-54}]$$

$$\boxed{h'^T = (1.082 \ 0.784 \ 0.784 \ 0.784) \text{ ft}}$$

### Weight of reduced reinforced area

$$W'_{ri_n} := L'_{s_n} \cdot E_n \cdot \gamma_i \quad [\text{Eq. 5-55}]$$

$$\boxed{W'^T_{ri} = (2826 \ 3336 \ 4513 \ 5690) \cdot \text{plf}}$$

### Weight of wedge beyond reinforced soil zone

$$W'_{r\beta_n} := \frac{1}{2} \cdot \left( L_{s\beta_n} \cdot h'_n \right) \cdot \gamma_i \quad [\text{Eq. 5-56}]$$

$$\boxed{W'^T_{r\beta} = (365.04 \ 191.78 \ 191.78 \ 191.78) \cdot \text{plf}}$$

### Friction developed by weight

$$R'_{s_n} := C_{dsi} \cdot \left[ q_d \cdot \left( L_{s\beta_n} + Z \right) + W'_{ri_n} + W'_{r\beta_n} \right] \cdot \tan(\phi_i) \quad [\text{Eq. 5-49}]$$

$$\boxed{R'^T_s = (1595 \ 1764 \ 2352 \ 2940) \cdot \text{plf}}$$

### Shear capacity of facing elements

$$V_{u_n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$\boxed{V_u^T = (1489 \ 1677 \ 1864 \ 1895) \cdot \text{plf}}$$

### Driving Forces

From retained soil

$$P_{s_n} := \left[ \frac{1}{2} \cdot K_a e \cdot \gamma_e \cdot (E_n + h'_n)^2 \cdot \cos(\delta_e - \omega) \right] \quad [\text{Eq. 5-6}]$$

$$\boxed{P_s^T = (435 \ 802 \ 1376 \ 2104) \cdot \text{plf}}$$

From surcharge

$$P_{q_n} := (q_d + q_l) \cdot K_a e \cdot (E_n + h'_n) \cdot \cos(\delta_e - \omega) \quad [\text{Eq. 5-8}]$$

$$\boxed{P_q^T = (0 \ 0 \ 0 \ 0) \cdot \text{plf}}$$

### Factor of safety against internal sliding

$$P_{a_n} := P_{s_n} + P_{q_n} \quad [\text{Eq. 5-11}]$$

$$\boxed{P_a^T = (435 \ 802 \ 1376 \ 2104) \cdot \text{plf}}$$

$$FS_{sl_n} := \frac{R'_{s_n} + V_{u_n}}{(P_{a_n})} \quad [\text{Eq. 5-48}]$$

$$\boxed{FS_{sl}^T = (7.096 \ 4.29 \ 3.064 \ 2.298)}$$

## Local Stability of Facing Units

### Facing Connection Strength

$$T_{conn,n} := \min \left[ V_{csmax,n}, a_{cs,n} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs,n}) \right] \quad [\text{Eq. 5-59}]$$

$$T_{conn}^T = (1489 \ 1677 \ 1864 \ 1895) \cdot \text{plf}$$

$$FS_{conn,n} := \frac{T_{conn,n}}{F_{g,n}} \quad FS_{conn}^T = (5.003 \ 5.417 \ 4.452 \ 3.03)$$

### Resistance to Bulging

Shear capacity at each geogrid layer

$$V_{u,n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$V_u^T = (1489 \ 1677 \ 1864 \ 1895) \cdot \text{plf}$$

Driving Force at each geogrid layer

$$P_{a,n} := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (E_n)^2 \cdot \cos(\delta_i - \omega) \right] + (q_d + q_l) \cdot K_{a,i} \cdot (E_n) \cdot \cos(\delta_i - \omega) \quad [\text{Eq. 5-11}]$$

$$P_a^T = (184 \ 439 \ 803 \ 1276) \cdot \text{plf}$$

Sum of tension in reinforcement layers above layer being considered

$$F_{n+1} := \sum_{i=1}^n F_{g,i}$$

$$F^T = (0 \ 298 \ 607 \ 1026 \ 1651) \cdot \text{plf}$$

$$FS_{sc,n} := \frac{V_{u,n}}{P_{a,n} - F_n} \quad [\text{Eq. 5-61}]$$

$$FS_{sc}^T = (8.101 \ 11.881 \ 9.525 \ 7.572)$$

### Maximum unreinforced height of SRW units

$$y := E_1 = 3.67 \text{ ft}$$

$$q_w := 0 \cdot \text{psf}$$

Moment equilibrium

Driving Moments

$$P'_s := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (y)^2 \cdot \cos(\delta_i - \omega) \right] \quad [\text{Eq. 4-5}]$$

$$P'_s = 183.809 \cdot \text{plf}$$

$$P'_q := (q_d + q_l) \cdot K_{a_i} \cdot (y) \cdot \cos(\delta_i - \omega)$$
[Eq. 4-6]

$$P'_q = 0 \cdot \text{plf}$$

$$P'_a := P'_s + P'_q$$
[Eq. 4-4]

$$P'_a = 183.809 \cdot \text{plf}$$

$$Y'_s := \frac{1}{3} \cdot y$$
[Eq. 4-7]

$$Y'_s = 1.223 \text{ ft}$$

$$Y'_q := \frac{1}{2} \cdot y$$
[Eq. 4-8]

$$Y'_q = 1.84 \text{ ft}$$

$$M'_o := P'_s \cdot Y'_s + P'_q \cdot Y'_q$$
[Eq. 4-17]

$$M'_o = 224.86 \cdot \text{lbf}$$

### Resisting Moments

$$W'_w := y \cdot \gamma_u \cdot W_u$$
[Eq. 4-9]

$$W'_w = 440.4 \cdot \text{plf}$$

$$X'_w := G_u + \frac{1}{2} \cdot (y) \cdot \tan(\omega)$$
[Eq. 4-16]

$$X'_w = 0.729 \text{ ft}$$

$$M'_r := W'_w \cdot X'_w$$
[Eq. 4-15]

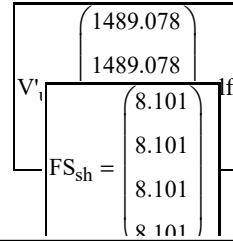
$$M'_r = 321.217 \text{ ft} \cdot \text{plf}$$

$$FS_{ot} := \frac{M'_r}{M'_o}$$
[Eq. 4-14]

$$FS_{ot} = 1.429$$

### Factor of Safety against Shear failure

$$V'_u := a_{cs} + W'_w \cdot \tan(\lambda_{cs})$$
[Eq. 4-25]



$$FS_{sh} := \frac{V'_u}{P'_a}$$
[Eq. 4-27]

## Summary

Wall Height

$$H = 11 \text{ ft}$$

Unreinforced Stability

$$FS_{ot} = 1.429$$

$$FS_{bearing} = 4.683$$

Applied Bearing Stress

$$Q_a = 1372 \cdot \text{psf}$$

Grid Elevation	Geogrid Length	Tensile Force	Geogrid Strength	Anch. Length	Anch. Capacity	FS Grid Tension (1.0)	FS Pullout (1.5)	FS Int Sliding (1.5)	FS Conn (1.5)	FS Bulging (1.5)
$E_n =$	$L_n =$	$\frac{F_{g_n}}{\text{plf}} =$	$\frac{T_{a_n}}{\text{plf}} =$	$L_{a_n} =$	$\frac{AC_n}{\text{plf}} =$	$FS_{ten\_n} =$	$FS_{po\_n} =$	$FS_{sl\_n} =$	$FS_{conn\_n} =$	$FS_{sc\_n} =$
3.67	ft	8	ft	298	834	1.58	668	2.8	2.24	7.1
5.67		8		310	834	2.87	1722	2.69	5.56	4.29
7.67		8		419	834	4.16	3233	1.99	7.72	3.06
9.67		8		625	834	5.45	5202	1.33	8.32	2.3

# Segmental Retaining Wall Design Calculations per NCMA

## Wall Geometry

Height $H_{\text{av}} := 9.0 \cdot \text{ft}$	Backslope $\beta := 10.0 \cdot \text{deg}$	Dead Load $q_d := 0 \cdot \text{psf}$	Live Load $q_l := 0 \cdot \text{psf}$	Distance to Slope $Z := 1.0 \cdot \text{ft}$	Wall below grade at toe $H_{\text{cmb}} := .67 \cdot \text{ft}$
--	---	--	--	---	--

## Soil Properties

Reinforced Soil (Internal) $\gamma_i := 110 \cdot \text{pcf}$ $\phi_i := 32 \cdot \text{deg}$ $C_{\text{dsi}} := 0.8$	Retained Soil (External) $\gamma_e := 120 \cdot \text{pcf}$ $\phi_e := 26 \cdot \text{deg}$ $C_{\text{dse}} := 1.0$	Drainage Fill $\gamma_d := 110 \cdot \text{pcf}$ $\phi_d := 32 \cdot \text{deg}$	Foundation Soil $\gamma_f := 120 \cdot \text{pcf}$ $\phi_f := 26 \cdot \text{deg}$ $c_f := 0.0 \text{ psf}$	Pullout $C_i := 0.7$
---	---	--	--	-------------------------

## Segmental Unit Properties

Height $H_u := 8 \cdot \text{in}$	Length $L_u := 18 \cdot \text{in}$	Width $W_u := 12 \cdot \text{in}$	Setback $\Delta_u := 1.0 \cdot \text{in}$	Center of Gravity $G_u := 6 \cdot \text{in}$	Batter $\omega := \tan\left(\frac{\Delta_u}{H_u}\right)$ $\omega = 7.125 \cdot \text{deg}$
Infilled Unit Weight $\gamma_u := 120 \cdot \text{pcf}$	Hinge Height $H_h := \text{if} \left[ \tan(\omega) = 0, H, \left[ 2 \cdot \frac{(W_u - G_u)}{\tan(\omega)} \right] \right] \Rightarrow H_h = 8 \text{ ft}$				[Eq. 4-1]

### Internal Interface Friction Angle

$$\delta_i := \frac{2}{3} \cdot \phi_i \quad [\delta_i = 21.33 \cdot \text{deg}] \quad [\text{Eq. 3-17}]$$

### Internal Active Earth Pressure

$$K_{a_i} := \frac{\cos(\phi_i + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_i) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_i + \delta_i) \cdot \sin(\phi_i - \beta)}{\cos(\omega - \delta_i) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{a_i} = 0.256]$$

### External Interface Friction Angle

$$\delta_e := \text{if}(\phi_i > \phi_e, \phi_e, \phi_i) \quad [\delta_e = 26 \cdot \text{deg}] \quad [\text{Eq. 3-16}]$$

### External Active Earth Pressure

$$K_{a_e} := \frac{\cos(\phi_e + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_e) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_e + \delta_e) \cdot \sin((\phi_e - \beta))}{\cos(\omega - \delta_e) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{a_e} = 0.339]$$

### Orientation of Critical Internal Failure Surface

$$\alpha_i := \text{atan} \left[ \frac{-\tan(\phi_i - \beta) + \sqrt{(\tan(\phi_i - \beta)) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega)) \cdot (1 + \tan(\delta_i - \omega) \cdot \cot(\phi_i + \omega))}}{1 + \tan(\delta_i - \omega) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega))} \right] + \phi_i \quad [\text{Eq. 3-14}] \quad [\alpha_i = 52.419 \cdot \text{deg}]$$

### Orientation of Critical External Failure Surface

$$\alpha_e := \text{atan} \left[ \frac{-\tan(\phi_e - \beta) + \sqrt{\tan(\phi_e - \beta) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega)) \cdot (1 + \tan(\delta_e - \omega) \cdot \cot(\phi_e + \omega))}}{1 + \tan(\delta_e - \omega) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega))} \right] + \phi_e \quad [\text{Eq. 3-14}] \quad [\alpha_e = 46.452 \cdot \text{deg}]$$

**Sliding****External Stability Analysis**

Given

$$\min \left[ \frac{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_e)}{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_d)} \right. \\ \left. C_{dse} \cdot c_f \cdot L + \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_f) \right] \cdot \tan(\beta) \right] \\ 1.5 = \frac{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \dots + (q_d + q_l) \cdot K_a_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]}{1.5}$$

**Overspinning**

$L_{sliding} := \text{Find}(L)$

$L_{sliding} = 4.885 \text{ ft}$

Given

$$2.0 = \frac{\left[ (L \cdot \gamma_e \cdot H) \cdot \left[ \frac{1}{2} \cdot (L + H \cdot \tan(\omega)) \right] \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \cdot \left[ H \cdot \tan(\omega) + W_u + Z + \frac{2}{3} \cdot (L - W_u - Z) \right] + q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \frac{Z + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right]}{2} + H \cdot \tan(\omega) + \right]}{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \cdot \left[ \frac{1}{3} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{2} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right] \cdot \cos(\delta_e - \omega) \right]}$$

$L_{overspinning} := \text{Find}(L)$

$L_{overspinning} = 3.834 \text{ ft}$

$$L := \max \begin{pmatrix} L_{sliding} \\ L_{overspinning} \\ 0.6 \cdot H \end{pmatrix}$$

$L = 5.4 \text{ ft}$

Based on Overspinning and Sliding:

$L := 7.0 \text{ ft}$  (Round up L)

## Eccentricity

$$L' := L - W_u - Z$$

$$L' = 5 \text{ ft}$$

[Fig. 2-10] [Eq. 5-1]

$$L'' := \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)}$$

$$L'' = 0.113 \text{ ft}$$

[Fig. 2-10] [Eq. 5-2]

$$L_\beta := L' + L''$$

$$L_\beta = 5.113 \text{ ft}$$

[Fig. 2-10] [Eq. 5-3]

$$h := L_\beta \cdot \tan(\beta)$$

$$h = 0.902 \text{ ft}$$

[Fig. 2-10] [Eq. 5-4]

$$W_{ri} := L \cdot \gamma_i \cdot H$$

$$W_{ri} = 6930 \cdot \text{plf}$$

[Eq. 5-15]

$$X_{ri} := \frac{1}{2} \cdot (L + H \cdot \tan(\omega))$$

$$X_{ri} = 4.063 \text{ ft}$$

[Eq. 5-19]

$$W_{r\beta} := \frac{1}{2} \cdot \gamma_i \cdot (L' - Z) \cdot h$$

$$W_{r\beta} = 198.331 \cdot \text{plf}$$

[Eq. 5-16]

$$X_{r\beta} := H \cdot \tan(\omega) + W_u + \frac{2}{3} \cdot L_\beta + Z$$

$$X_{r\beta} = 6.533 \text{ ft}$$

[Eq. 5-20]

$$X_{q\beta} := \frac{Z + L_\beta}{2} + [(H + h) \cdot \tan(\omega)] + W_u$$

$$X_{q\beta} = 5.294 \text{ ft}$$

[Eq. 5-21]

Actual Height of wall:

$$H_s := (H + h)$$

$$H_s = 9.902 \text{ ft}$$

Earth Pressures:

$$P_{sH} := \left[ \frac{1}{2} \cdot K_a e \cdot \gamma_e \cdot (H + h)^2 \cdot \cos(\delta_e - \omega) \right]$$

$$P_{sH} = 1887.145 \cdot \text{plf}$$

[Eq. 5-6]

$$Y_s := \frac{1}{3} \cdot (H + h)$$

$$Y_s = 3.301 \text{ ft}$$

[Eq. 5-9]

$$P_{qH} := (q_d + q_l) \cdot K_a e \cdot (H + h) \cdot \cos(\delta_e - \omega)$$

$$P_{qH} = 0 \cdot \text{plf}$$

[Eq. 5-8]

$$Y_q := \frac{1}{2} \cdot (H + h)$$

$$Y_q = 4.951 \text{ ft}$$

[Eq. 5-10]

$$\textcolor{brown}{e} := \frac{\left[ P_{sH} \cdot Y_s + P_{qH} \cdot Y_q - W_{ri} \cdot \left( X_{ri} - \frac{L}{2} \right) - W_{r\beta} \cdot \left( X_{r\beta} - \frac{L}{2} \right) - q_d \cdot (L_\beta) \cdot \left( X_{q\beta} - \frac{L}{2} \right) \right]}{W_{ri} + W_{r\beta} + q_d \cdot (L_\beta)}$$

$$e = 0.2425 \text{ ft}$$

[Eq. 5-25]

Check  $\textcolor{brown}{e} := \text{if}(e \leq 0, 0.075L, e)$

$$e = 0.243 \text{ ft}$$

Surcharge is applied over:

$$(L' + L'') = 5.113 \text{ ft}$$

$$B := L - 2 \cdot e$$

$$B = 6.515 \text{ ft}$$

[Eq. 5-24]

## Bearing Capacity

$$Q_a := \frac{[W_{ri} + W_{rf\beta} + (q_d + q_l) \cdot (L' + L'')]}{B}$$

$$Q_a = 1094.148 \cdot \text{psf}$$

$$N_q := \tan\left(45^\circ - \frac{\phi_f}{2}\right)^2 \cdot \exp(\pi \cdot \tan(\phi_f))$$

$$N_q = 11.854$$

[Fig. 4-5]

$$N_c := \text{if } [\phi_f = 0, 5.14, (N_q - 1) \cdot \cot(\phi_f)]$$

$$N_c = 22.254$$

[Fig. 4-5]

$$N_\gamma := 2 \cdot (N_q + 1) \cdot \tan(\phi_f)$$

$$N_\gamma = 12.539$$

[Fig. 4-5]

$$Q_{ult} := c_f \cdot N_c + \frac{1}{2} \cdot \gamma_f \cdot B \cdot N_\gamma + \gamma_f \cdot H_{emb} \cdot N_q$$

$$Q_{ult} = 5854.474 \cdot \text{psf}$$

[Eq. 4-20]

$$FS_{bearing} := \frac{Q_{ult}}{Q_a}$$

$$FS_{bearing} = 5.351$$

[Eq. 4-19]

## Internal Stability

### Reinforcement Properties

#### Geogrid Design Data

Backfill Soil      Type := (gravel)

1    2    3    4    5    6    7    8    9

Geogrid Number

$$\text{Type}^T = (411 \ 834 \ 1199 \ 1336 \ 2004 \ 2508 \ 3011 \ 3873 \ 7914)$$

$$GN1 := 4$$

$$GN2 := 2$$

$$\text{inter}^T = (1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 0)$$

$$\text{slope}^T = (38 \ 38 \ 38 \ 38 \ 38 \ 38 \ 0)$$

$$\text{maxc}^T = (4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 0) \quad x := 4..1 \quad x \text{ is the number of grids at the top of the wall of a different type}$$

$$T_a := \text{Type}_{GN1} \cdot \text{plf} \quad T_a = 1336 \cdot \text{plf}$$

$$T_{a2} := \text{Type}_{GN2} \cdot \text{plf} \quad T_{a2} = 834 \cdot \text{plf}$$

$$a_{cs} := \text{inter}_{GN1} \cdot \text{plf} \quad a_{cs} = 1145 \cdot \text{plf}$$

$$\lambda_{cs} := \text{slope}_{GN1} \cdot \text{deg} \quad \lambda_{cs} = 38 \cdot \text{deg}$$

$$V_{csmax} := \text{maxc}_{GN1} \cdot \text{plf} \quad V_{csmax} = 4540 \cdot \text{plf}$$

$$a_{cs2} := \text{inter}_{GN2} \cdot \text{plf} \quad a_{cs2} = 1145 \cdot \text{plf}$$

$$\lambda_{cs2} := \text{slope}_{GN2} \cdot \text{deg} \quad \lambda_{cs2} = 38 \cdot \text{deg}$$

$$V_{csmax2} := \text{maxc}_{GN2} \cdot \text{plf} \quad V_{csmax2} = 4540 \cdot \text{plf}$$

## Tension in Geogrid

Number of Grids:	Grig Spacing (ft):	# of grids for that spacing:	Depth of first grid (ft):	Length of grids:
$n_g := 3$	$Spacing1 := 2$	$n_1 := 3$	$h_1 := 3.67$	$L_1 := 7.0 \quad L_2 := 7.0 \quad L_t := \frac{L}{ft}$
	$Spacing2 := 1.67$	$n_2 := 0$		

Make all zero when using one geogrid

Note: make sure that the elevations don't exceed the height of the wall (H)  $H = 9$  ft

$$\begin{aligned} top &:= \text{length}(E) & p &:= 2..top & top &= 3 \\ \text{grids} &:= \text{length}(E) & n &:= 1..top & l &:= 1.. \text{grids} - 1 \end{aligned}$$

$$E = \begin{pmatrix} 3.67 \\ 5.67 \\ 7.67 \end{pmatrix} \text{ ft}$$

$$\begin{aligned} T_a^T &:= T_{a2} & T_{a_x} &= \begin{pmatrix} 834 \\ 834 \\ 834 \\ 834 \end{pmatrix} \cdot \text{plf} & \xrightarrow{\longrightarrow} T_a &:= \frac{L \cdot T_a}{L} \\ & & & & T_a &= \begin{pmatrix} 1336 \\ 1336 \\ 1336 \end{pmatrix} \cdot \text{plf} \end{aligned}$$

$$L = \begin{pmatrix} 7 \\ 7 \\ 7 \end{pmatrix} \text{ ft}$$

$$T_a^T = (834 \ 834 \ 834 \ 834) \cdot \text{plf}$$

$$D_p := \frac{E_{p-1} + E_p}{2} \quad D_1 := 0 \cdot \text{ft} \quad D_{\text{grids}+1} := H$$

$$D^T = (0 \ 4.67 \ 6.67 \ 9) \text{ ft}$$

### Total Applied Tensile Strength in the Geosynthetic reinf.:

$$F_{g_n} := \int_{D_n}^{D_{(n+1)}} (\gamma_i \cdot D + q_l + q_d) \cdot K_a \cdot \cos(\delta_i - \omega) \, dD \quad [\text{Eq. 5-36}]$$

$$F_g^T = (297.624 \ 309.512 \ 498.264) \cdot \text{plf}$$

### Safety factor:

$$FS_{ten} := \frac{T_{a_n}}{F_{g_n}} \quad FS_{ten}^T = (2.802 \ 2.695 \ 1.674)$$

## Pullout Capacity

### Anchorage Length of Geosynthetic

$$La_n := L_n - W_u - [(H + h) - E_n] \cdot \tan(90^\circ - \alpha_i) + [(H + h) - E_n] \cdot \tan(\omega) \quad [\text{Eq. 5-46}]$$

$$La^T = (1.983 \ 3.272 \ 4.562) \text{ ft}$$

**Note:** If the anchorage length is less than 1ft then there is not enough embedment length and it has to be increased. Note that in some cases it might just be the top two grids.

### Average Depth of overburden on Anchorage length

$$d_n := E_n + \left[ (H - E_n) \cdot \tan(90^\circ - \alpha_i) + \frac{La_n}{2} - (Z + H \cdot \tan(\omega) - \Delta_u) \right] \cdot \tan(\beta) \quad [\text{Eq. 5-47}]$$

$$d^T = (4.208 \ 6.05 \ 7.893) \text{ ft}$$

### Anchorage Capacity

$$AC_n := 2 \cdot La_n \cdot C_i \cdot (d_n \cdot \gamma_i + q_d) \cdot \tan(\phi_i) \quad [\text{Eq. 5-45}]$$

$$AC^T = (803.122 \ 1905.307 \ 3464.58) \cdot \text{plf}$$

$$F_g^T = (297.624 \ 309.512 \ 498.264) \cdot \text{plf}$$

### Safety Factor

$$FS_{po} := \frac{\overrightarrow{AC}}{F_g} \quad [\text{Eq. 5-44}]$$

$$FS_{po}^T = (2.698 \ 6.156 \ 6.953)$$

## Internal Sliding

### Reduced reinforcement length

$$\Delta L_{l+1} := \begin{cases} \left[ (E_{l+1} - E_l) \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) \right] & \text{if } n_g > 2 \\ \text{Spacing1} \cdot \text{ft} \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) & \text{if } n_g = 2 \\ 0 & \text{if } n_g = 1 \end{cases} \quad [\text{Eq. 5-51}]$$

$$\Delta L^T = (0 \ 1.651 \ 1.651) \text{ ft}$$

$$L'_{s_n} := L_n - W_u - \Delta L_n \quad [\text{Eq. 5-50}]$$

$$L'_s^T = (6 \ 4.349 \ 4.349) \text{ ft}$$

### Length of sloping ground

$$L_{s\beta_n} := L'_{s_n} + \frac{(L'_{s_n} - W_u) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} - Z \quad [\text{Eq. 5-53 & 5-52}]$$

$$\boxed{L_{s\beta}^T = (5.113 \quad 3.424 \quad 3.424) \text{ ft}}$$

### Height of slope above crest of wall

$$h'_n := L_{s\beta} \cdot \tan(\beta) \quad [\text{Eq. 5-54}]$$

$$\boxed{h'^T = (0.902 \quad 0.604 \quad 0.604) \text{ ft}}$$

### Weight of reduced reinforced area

$$W'_{ri} := L'_s \cdot E_n \cdot \gamma_i \quad [\text{Eq. 5-55}]$$

$$\boxed{W'^T_{ri} = (2422 \quad 2712 \quad 3669) \cdot \text{plf}}$$

### Weight of wedge beyond reinforced soil zone

$$W'_{r\beta} := \frac{1}{2} \cdot \left( L_{s\beta} \cdot h'_n \right) \cdot \gamma_i \quad [\text{Eq. 5-56}]$$

$$\boxed{W'^T_{r\beta} = (253.5 \quad 113.72 \quad 113.72) \cdot \text{plf}}$$

### Friction developed by weight

$$R'_s := C_{dsi} \cdot \left[ q_d \cdot \left( L_{s\beta} + Z \right) + W'_{ri} + W'_{r\beta} \right] \cdot \tan(\phi_i) \quad [\text{Eq. 5-49}]$$

$$\boxed{R'^T_s = (1338 \quad 1413 \quad 1891) \cdot \text{plf}}$$

### Shear capacity of facing elements

$$V_{u_n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$\boxed{V_u^T = (1489 \quad 1677 \quad 1864) \cdot \text{plf}}$$

### Driving Forces

From retained soil

$$P_s := \left[ \frac{1}{2} \cdot K_a \cdot \gamma_e \cdot (E_n + h'_n)^2 \cdot \cos(\delta_e - \omega) \right] \quad [\text{Eq. 5-6}]$$

$$\boxed{P_s^T = (402 \quad 758 \quad 1318) \cdot \text{plf}}$$

From surcharge

$$P_q := (q_d + q_l) \cdot K_a \cdot (E_n + h'_n) \cdot \cos(\delta_e - \omega) \quad [\text{Eq. 5-8}]$$

$$\boxed{P_q^T = (0 \quad 0 \quad 0) \cdot \text{plf}}$$

### Factor of safety against internal sliding

$$P_a := P_s + P_q \quad [\text{Eq. 5-11}]$$

$$\boxed{P_a^T = (402 \quad 758 \quad 1318) \cdot \text{plf}}$$

$$FS_{sl} := \frac{R'_s + V_{u_n}}{(P_a)} \quad [\text{Eq. 5-48}]$$

$$\boxed{FS_{sl}^T = (7.027 \quad 4.078 \quad 2.85)}$$

## Local Stability of Facing Units

### Facing Connection Strength

$$T_{conn,n} := \min[V_{csmax,n}, a_{cs,n} + (\text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u) \cdot \tan(\lambda_{cs,n})] \quad [\text{Eq. 5-59}]$$

$$T_{conn}^T = (1489 \quad 1677 \quad 1864) \cdot \text{plf}$$

$$FS_{conn,n} := \frac{T_{conn,n}}{F_{g,n}} \quad FS_{conn}^T = (5.003 \quad 5.417 \quad 3.741)$$

### Resistance to Bulging

Shear capacity at each geogrid layer

$$V_{u,n} := \min[V_{csmax}, a_{cs} + (\text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u) \cdot \tan(\lambda_{cs})] \quad [\text{Eq. 4-25}]$$

$$V_u^T = (1489 \quad 1677 \quad 1864) \cdot \text{plf}$$

Driving Force at each geogrid layer

$$P_{a,n} := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (E_n)^2 \cdot \cos(\delta_i - \omega) \right] + (q_d + q_l) \cdot K_{a,i} \cdot (E_n) \cdot \cos(\delta_i - \omega) \quad [\text{Eq. 5-11}]$$

$$P_a^T = (184 \quad 439 \quad 803) \cdot \text{plf}$$

Sum of tension in reinforcement layers above layer being considered

$$F_{n+1} := \sum_{i=1}^n F_{g,i}$$

$$F^T = (0 \quad 298 \quad 607 \quad 1105) \cdot \text{plf}$$

$$FS_{sc,n} := \frac{V_{u,n}}{P_{a,n} - F_n} \quad [\text{Eq. 5-61}]$$

$$FS_{sc}^T = (8.101 \quad 11.881 \quad 9.525)$$

### Maximum unreinforced height of SRW units

$$y := E_1 = 3.67 \text{ ft}$$

$$\gamma_w := 0 \cdot \text{psf}$$

Moment equilibrium

Driving Moments

$$P'_s := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (y)^2 \cdot \cos(\delta_i - \omega) \right] \quad [\text{Eq. 4-5}]$$

$$P'_s = 183.809 \cdot \text{plf}$$

$$P'_q := (q_d + q_l) \cdot K_{a_i} \cdot (y) \cdot \cos(\delta_i - \omega)$$
[Eq. 4-6]

$$P'_q = 0 \cdot \text{plf}$$

$$P'_a := P'_s + P'_q$$
[Eq. 4-4]

$$P'_a = 183.809 \cdot \text{plf}$$

$$Y'_s := \frac{1}{3} \cdot y$$
[Eq. 4-7]

$$Y'_s = 1.223 \text{ ft}$$

$$Y'_q := \frac{1}{2} \cdot y$$
[Eq. 4-8]

$$Y'_q = 1.84 \text{ ft}$$

$$M'_o := P'_s \cdot Y'_s + P'_q \cdot Y'_q$$
[Eq. 4-17]

$$M'_o = 224.86 \cdot \text{lbf}$$

### Resisting Moments

$$W'_w := y \cdot \gamma_u \cdot W_u$$
[Eq. 4-9]

$$W'_w = 440.4 \cdot \text{plf}$$

$$X'_w := G_u + \frac{1}{2} \cdot (y) \cdot \tan(\omega)$$
[Eq. 4-16]

$$X'_w = 0.729 \text{ ft}$$

$$M'_r := W'_w \cdot X'_w$$
[Eq. 4-15]

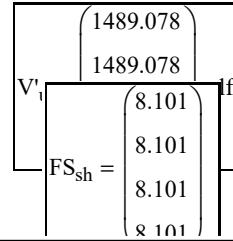
$$M'_r = 321.217 \text{ ft} \cdot \text{plf}$$

$$FS_{ot} := \frac{M'_r}{M'_o}$$
[Eq. 4-14]

$$FS_{ot} = 1.429$$

### Factor of Safety against Shear failure

$$V'_u := a_{cs} + W'_w \cdot \tan(\lambda_{cs})$$
[Eq. 4-25]



$$FS_{sh} := \frac{V'_u}{P'_a}$$
[Eq. 4-27]

## Summary

Wall Height

$$H = 9 \text{ ft}$$

Unreinforced Stability

$$FS_{ot} = 1.429$$

$$FS_{bearing} = 5.351$$

Applied Bearing Stress

$$Q_a = 1094 \cdot \text{psf}$$

Grid Elevation	Geogrid Length	Tensile Force	Geogrid Strength	Anch. Length	Anch. Capacity	FS Grid Tension (1.0)	FS Pullout (1.5)	FS Int Sliding (1.5)	FS Conn (1.5)	FS Bulging (1.5)
$E_n =$	$L_n =$	$\frac{F_{g_n}}{\text{plf}} =$	$\frac{T_{a_n}}{\text{plf}} =$	$L_{a_n} =$	$\frac{AC_n}{\text{plf}} =$	$FS_{ten\_n} =$	$FS_{po\_n} =$	$FS_{sl\_n} =$	$FS_{conn\_n} =$	$FS_{sc\_n} =$
3.67	ft	7	298	834	1.98	803	2.8	2.7	7.03	5
5.67		7	310	834	3.27	1905	2.69	6.16	4.08	5.42
7.67		7	498	834	4.56	3465	1.67	6.95	2.85	3.74

# Segmental Retaining Wall Design Calculations per NCMA

## Wall Geometry

Height $H_{\text{av}} := 7.0 \cdot \text{ft}$	Backslope $\beta := 10.0 \cdot \text{deg}$	Dead Load $q_d := 0 \cdot \text{psf}$	Live Load $q_l := 0 \cdot \text{psf}$	Distance to Slope $Z := 1.0 \cdot \text{ft}$	Wall below grade at toe $H_{\text{cmb}} := .67 \cdot \text{ft}$
--	---	--	--	---	--

## Soil Properties

Reinforced Soil (Internal) $\gamma_i := 110 \cdot \text{pcf}$ $\phi_i := 32 \cdot \text{deg}$ $C_{\text{dsi}} := 0.8$	Retained Soil (External) $\gamma_e := 120 \cdot \text{pcf}$ $\phi_e := 26 \cdot \text{deg}$ $C_{\text{dse}} := 1.0$	Drainage Fill $\gamma_d := 110 \cdot \text{pcf}$ $\phi_d := 32 \cdot \text{deg}$	Foundation Soil $\gamma_f := 120 \cdot \text{pcf}$ $\phi_f := 26 \cdot \text{deg}$ $c_f := 0.0 \text{ psf}$	Pullout $C_i := 0.7$
---	---	--	--	-------------------------

## Segmental Unit Properties

Height $H_u := 8 \cdot \text{in}$	Length $L_u := 18 \cdot \text{in}$	Width $W_u := 12 \cdot \text{in}$	Setback $\Delta_u := 1.0 \cdot \text{in}$	Center of Gravity $G_u := 6 \cdot \text{in}$	Batter $\omega := \tan\left(\frac{\Delta_u}{H_u}\right)$ $\omega = 7.125 \cdot \text{deg}$
Infilled Unit Weight $\gamma_u := 120 \cdot \text{pcf}$	Hinge Height $H_h := \text{if} \left[ \tan(\omega) = 0, H, \left[ 2 \cdot \frac{(W_u - G_u)}{\tan(\omega)} \right] \right] \Rightarrow H_h = 8 \text{ ft}$				[Eq. 4-1]

### Internal Interface Friction Angle

$$\delta_i := \frac{2}{3} \cdot \phi_i \quad [\delta_i = 21.33 \cdot \text{deg}] \quad [\text{Eq. 3-17}]$$

### Internal Active Earth Pressure

$$K_{a_i} := \frac{\cos(\phi_i + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_i) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_i + \delta_i) \cdot \sin(\phi_i - \beta)}{\cos(\omega - \delta_i) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{a_i} = 0.256]$$

### External Interface Friction Angle

$$\delta_e := \text{if}(\phi_i > \phi_e, \phi_e, \phi_i) \quad [\delta_e = 26 \cdot \text{deg}] \quad [\text{Eq. 3-16}]$$

### External Active Earth Pressure

$$K_{a_e} := \frac{\cos(\phi_e + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_e) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_e + \delta_e) \cdot \sin((\phi_e - \beta))}{\cos(\omega - \delta_e) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{a_e} = 0.339]$$

### Orientation of Critical Internal Failure Surface

$$\alpha_i := \text{atan} \left[ \frac{-\tan(\phi_i - \beta) + \sqrt{(\tan(\phi_i - \beta)) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega)) \cdot (1 + \tan(\delta_i - \omega) \cdot \cot(\phi_i + \omega))}}{1 + \tan(\delta_i - \omega) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega))} \right] + \phi_i \quad [\text{Eq. 3-14}] \quad [\alpha_i = 52.419 \cdot \text{deg}]$$

### Orientation of Critical External Failure Surface

$$\alpha_e := \text{atan} \left[ \frac{-\tan(\phi_e - \beta) + \sqrt{\tan(\phi_e - \beta) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega)) \cdot (1 + \tan(\delta_e - \omega) \cdot \cot(\phi_e + \omega))}}{1 + \tan(\delta_e - \omega) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega))} \right] + \phi_e \quad [\text{Eq. 3-14}] \quad [\alpha_e = 46.452 \cdot \text{deg}]$$

**Sliding****External Stability Analysis**

Given

$$\min \left[ \frac{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_e)}{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_d)} \right. \\ \left. \frac{C_{dse} \cdot c_f \cdot L + \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_f)}{1.5 = \left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \dots + (q_d + q_l) \cdot K_a_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]} \right]$$

**Overspinning**

$L_{sliding} := \text{Find}(L)$

$L_{sliding} = 3.729 \text{ ft}$

Given

$$2.0 = \frac{\left[ (L \cdot \gamma_e \cdot H) \cdot \left[ \frac{1}{2} \cdot (L + H \cdot \tan(\omega)) \right] \right] \dots + \left[ \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \left[ H \cdot \tan(\omega) + W_u + Z + \frac{2}{3} \cdot (L - W_u - Z) \right] + q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \frac{Z + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right]}{2} + H \cdot \tan(\omega) +}{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{3} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{2} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]}$$

$L_{overspinning} := \text{Find}(L)$

$L_{overspinning} = 2.934 \text{ ft}$

$$L := \max \begin{pmatrix} L_{sliding} \\ L_{overspinning} \\ 0.6 \cdot H \end{pmatrix}$$

$L = 4.2 \text{ ft}$

Based on Overspinning and Sliding:

$L := 5.0 \text{ ft}$  (Round up L)

## Eccentricity

$$L' := L - W_u - Z$$

$$L' = 3 \text{ ft}$$

[Fig. 2-10] [Eq. 5-1]

$$L'' := \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)}$$

$$L'' = 0.068 \text{ ft}$$

[Fig. 2-10] [Eq. 5-2]

$$L_\beta := L' + L''$$

$$L_\beta = 3.068 \text{ ft}$$

[Fig. 2-10] [Eq. 5-3]

$$h := L_\beta \cdot \tan(\beta)$$

$$h = 0.541 \text{ ft}$$

[Fig. 2-10] [Eq. 5-4]

$$W_{ri} := L \cdot \gamma_i \cdot H$$

$$W_{ri} = 3850 \cdot \text{plf}$$

[Eq. 5-15]

$$X_{ri} := \frac{1}{2} \cdot (L + H \cdot \tan(\omega))$$

$$X_{ri} = 2.938 \text{ ft}$$

[Eq. 5-19]

$$W_{r\beta} := \frac{1}{2} \cdot \gamma_i \cdot (L' - Z) \cdot h$$

$$W_{r\beta} = 59.499 \cdot \text{plf}$$

[Eq. 5-16]

$$X_{r\beta} := H \cdot \tan(\omega) + W_u + \frac{2}{3} \cdot L_\beta + Z$$

$$X_{r\beta} = 4.92 \text{ ft}$$

[Eq. 5-20]

$$X_{q\beta} := \frac{Z + L_\beta}{2} + [(H + h) \cdot \tan(\omega)] + W_u$$

$$X_{q\beta} = 3.976 \text{ ft}$$

[Eq. 5-21]

Actual Height of wall:

$$H_s := (H + h)$$

$$H_s = 7.541 \text{ ft}$$

Earth Pressures:

$$P_{sH} := \left[ \frac{1}{2} \cdot K_a e \cdot \gamma_e \cdot (H + h)^2 \cdot \cos(\delta_e - \omega) \right]$$

$$P_{sH} = 1094.585 \cdot \text{plf}$$

[Eq. 5-6]

$$Y_s := \frac{1}{3} \cdot (H + h)$$

$$Y_s = 2.514 \text{ ft}$$

[Eq. 5-9]

$$P_{qH} := (q_d + q_l) \cdot K_a e \cdot (H + h) \cdot \cos(\delta_e - \omega)$$

$$P_{qH} = 0 \cdot \text{plf}$$

[Eq. 5-8]

$$Y_q := \frac{1}{2} \cdot (H + h)$$

$$Y_q = 3.77 \text{ ft}$$

[Eq. 5-10]

$$\frac{e := \left[ P_{sH} \cdot Y_s + P_{qH} \cdot Y_q - W_{ri} \cdot \left( X_{ri} - \frac{L}{2} \right) - W_{r\beta} \cdot \left( X_{r\beta} - \frac{L}{2} \right) - q_d \cdot (L_\beta) \cdot \left( X_{q\beta} - \frac{L}{2} \right) \right]}{W_{ri} + W_{r\beta} + q_d \cdot (L_\beta)}$$

$$e = 0.2361 \text{ ft}$$

[Eq. 5-25]

Check  $\frac{e}{\sqrt{3}} := \text{if}(e \leq 0, 0.075L, e)$

$$\frac{e}{\sqrt{3}} = 0.236 \text{ ft}$$

Surcharge is applied over:

$$(L' + L'') = 3.068 \text{ ft}$$

$$B := L - 2 \cdot e$$

$$B = 4.528 \text{ ft}$$

[Eq. 5-24]

## Bearing Capacity

$$Q_a := \frac{[W_{ri} + W_{rf\beta} + (q_d + q_l) \cdot (L' + L'')]}{B}$$

$$Q_a = 863.442 \cdot \text{psf}$$

$$N_q := \tan\left(45^\circ - \frac{\phi_f}{2}\right)^2 \cdot \exp(\pi \cdot \tan(\phi_f))$$

$$N_q = 11.854$$

[Fig. 4-5]

$$N_c := \text{if } [\phi_f = 0, 5.14, (N_q - 1) \cdot \cot(\phi_f)]$$

$$N_c = 22.254$$

[Fig. 4-5]

$$N_\gamma := 2 \cdot (N_q + 1) \cdot \tan(\phi_f)$$

$$N_\gamma = 12.539$$

[Fig. 4-5]

$$Q_{ult} := c_f \cdot N_c + \frac{1}{2} \cdot \gamma_f \cdot B \cdot N_\gamma + \gamma_f \cdot H_{emb} \cdot N_q$$

$$Q_{ult} = 4359.481 \cdot \text{psf}$$

[Eq. 4-20]

$$FS_{bearing} := \frac{Q_{ult}}{Q_a}$$

$$FS_{bearing} = 5.049$$

[Eq. 4-19]

## Internal Stability

### Reinforcement Properties

#### Geogrid Design Data

Backfill Soil      Type := (gravel)

1    2    3    4    5    6    7    8    9

Geogrid Number

$$\text{Type}^T = (411 \ 834 \ 1199 \ 1336 \ 2004 \ 2508 \ 3011 \ 3873 \ 7914)$$

$$GN1 := 4$$

$$GN2 := 2$$

$$\text{inter}^T = (1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 0)$$

$$\text{slope}^T = (38 \ 38 \ 38 \ 38 \ 38 \ 38 \ 0)$$

$$\text{maxc}^T = (4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 0) \quad x := 4..1 \quad x \text{ is the number of grids at the top of the wall of a different type}$$

$$T_a := \text{Type}_{GN1} \cdot \text{plf} \quad T_a = 1336 \cdot \text{plf}$$

$$T_{a2} := \text{Type}_{GN2} \cdot \text{plf} \quad T_{a2} = 834 \cdot \text{plf}$$

$$a_{cs} := \text{inter}_{GN1} \cdot \text{plf} \quad a_{cs} = 1145 \cdot \text{plf}$$

$$\lambda_{cs} := \text{slope}_{GN1} \cdot \text{deg} \quad \lambda_{cs} = 38 \cdot \text{deg}$$

$$V_{csmax} := \text{maxc}_{GN1} \cdot \text{plf} \quad V_{csmax} = 4540 \cdot \text{plf}$$

$$a_{cs2} := \text{inter}_{GN2} \cdot \text{plf} \quad a_{cs2} = 1145 \cdot \text{plf}$$

$$\lambda_{cs2} := \text{slope}_{GN2} \cdot \text{deg} \quad \lambda_{cs2} = 38 \cdot \text{deg}$$

$$V_{csmax2} := \text{maxc}_{GN2} \cdot \text{plf} \quad V_{csmax2} = 4540 \cdot \text{plf}$$

## Tension in Geogrid

Number of Grids:	Grig Spacing (ft):	# of grids for that spacing:	Depth of first grid (ft):	Length of grids:
$n_g := 3$	$Spacing1 := 2$	$n_1 := 3$	$h_1 := 3.67$	$L_1 := 5.0 \quad L_2 := 5.0 \quad L_t := \frac{L}{ft}$
	$Spacing2 := 1.67$	$n_2 := 0$		

Make all zero when using one geogrid

Note: make sure that the elevations don't exceed the height of the wall (H)  $H = 7$  ft

$$\begin{aligned} top &:= \text{length}(E) & p &:= 2..top & top &= 3 \\ \text{grids} &:= \text{length}(E) & n &:= 1..top & l &:= 1.. \text{grids} - 1 \end{aligned}$$

$$E = \begin{pmatrix} 3.67 \\ 5.67 \\ 7.67 \end{pmatrix} \text{ ft}$$

$$\begin{aligned} T_a^T &:= T_{a2} & T_{a_x} &= \begin{pmatrix} 834 \\ 834 \\ 834 \\ 834 \end{pmatrix} \cdot \text{plf} & \xrightarrow{\longrightarrow} T_a &:= \frac{L \cdot T_a}{L} \\ & & & & T_a &= \begin{pmatrix} 1336 \\ 1336 \\ 1336 \end{pmatrix} \cdot \text{plf} \end{aligned}$$

$$L = \begin{pmatrix} 5 \\ 5 \\ 5 \end{pmatrix} \text{ ft}$$

$$T_a^T = (834 \ 834 \ 834 \ 834) \cdot \text{plf}$$

$$D_p := \frac{E_{p-1} + E_p}{2} \quad D_1 := 0 \cdot \text{ft} \quad D_{\text{grids}+1} := H$$

$$D^T = (0 \ 4.67 \ 6.67 \ 7) \text{ ft}$$

### Total Applied Tensile Strength in the Geosynthetic reinf.:

$$F_{g_n} := \int_{D_n}^{D_{(n+1)}} (\gamma_i \cdot D + q_l + q_d) \cdot K a_i \cdot \cos(\delta_i - \omega) \, dD \quad [\text{Eq. 5-36}]$$

$$F_g^T = (297.624 \ 309.512 \ 61.563) \cdot \text{plf}$$

### Safety factor:

$$FS_{ten} := \frac{T_{a_n}}{F_{g_n}} \quad FS_{ten}^T = (2.802 \ 2.695 \ 13.547)$$

## Pullout Capacity

### Anchorage Length of Geosynthetic

$$La_n := L_n - W_u - [(H + h) - E_n] \cdot \tan(90^\circ - \alpha_i) + [(H + h) - E_n] \cdot \tan(\omega) \quad [\text{Eq. 5-46}]$$

$$\boxed{La^T = (1.505 \ 2.794 \ 4.083) \text{ ft}}$$

**Note:** If the anchorage length is less than 1ft then there is not enough embedment length and it has to be increased. Note that in some cases it might just be the top two grids.

### Average Depth of overburden on Anchorage length

$$d_n := E_n + \left[ (H - E_n) \cdot \tan(90^\circ - \alpha_i) + \frac{La_n}{2} - (Z + H \cdot \tan(\omega) - \Delta_u) \right] \cdot \tan(\beta) \quad [\text{Eq. 5-47}]$$

$$\boxed{d^T = (3.939 \ 5.781 \ 7.623) \text{ ft}}$$

### Anchorage Capacity

$$AC_n := 2 \cdot La_n \cdot C_i \cdot (d_n \cdot \gamma_i + q_d) \cdot \tan(\phi_i) \quad [\text{Eq. 5-45}]$$

$$\boxed{AC^T = (570.371 \ 1554.313 \ 2995.344) \cdot \text{plf}}$$

$$\boxed{F_g^T = (297.624 \ 309.512 \ 61.563) \cdot \text{plf}}$$

### Safety Factor

$$\overrightarrow{FS_{po}} := \frac{\overrightarrow{AC}}{\overrightarrow{F_g}} \quad [\text{Eq. 5-44}]$$

$$\boxed{FS_{po}^T = (1.916 \ 5.022 \ 48.655)}$$

## Internal Sliding

### Reduced reinforcement length

$$\Delta L_{l+1} := \begin{cases} \left[ (E_{l+1} - E_l) \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) \right] & \text{if } n_g > 2 \\ \text{Spacing1} \cdot \text{ft} \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) & \text{if } n_g = 2 \\ 0 & \text{if } n_g = 1 \end{cases} \quad [\text{Eq. 5-51}]$$

$$\boxed{\Delta L^T = (0 \ 1.651 \ 1.651) \text{ ft}}$$

$$L'_{s_n} := L_n - W_u - \Delta L_n \quad [\text{Eq. 5-50}]$$

$$\boxed{L'_s^T = (4 \ 2.349 \ 2.349) \text{ ft}}$$

### Length of sloping ground

$$L_{s\beta_n} := L'_{s_n} + \frac{(L'_{s_n} - W_u) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} - Z \quad [\text{Eq. 5-53 & 5-52}]$$

$$\boxed{L_{s\beta}^T = (3.068 \quad 1.379 \quad 1.379) \text{ ft}}$$

### Height of slope above crest of wall

$$h'_n := L_{s\beta} \cdot \tan(\beta) \quad [\text{Eq. 5-54}]$$

$$\boxed{h'^T = (0.541 \quad 0.243 \quad 0.243) \text{ ft}}$$

### Weight of reduced reinforced area

$$W'_{ri} := L'_s \cdot E_n \cdot \gamma_i \quad [\text{Eq. 5-55}]$$

$$\boxed{W'^T_{ri} = (1615 \quad 1465 \quad 1982) \cdot \text{plf}}$$

### Weight of wedge beyond reinforced soil zone

$$W'_{r\beta} := \frac{1}{2} \cdot \left( L_{s\beta} \cdot h'_n \right) \cdot \gamma_i \quad [\text{Eq. 5-56}]$$

$$\boxed{W'^T_{r\beta} = (91.26 \quad 18.45 \quad 18.45) \cdot \text{plf}}$$

### Friction developed by weight

$$R'_s := C_{dsi} \cdot \left[ q_d \cdot \left( L_{s\beta} + Z \right) + W'_{ri} + W'_{r\beta} \right] \cdot \tan(\phi_i) \quad [\text{Eq. 5-49}]$$

$$\boxed{R'^T_s = (853 \quad 742 \quad 1000) \cdot \text{plf}}$$

### Shear capacity of facing elements

$$V_{u_n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$\boxed{V_u^T = (1489 \quad 1677 \quad 1864) \cdot \text{plf}}$$

### Driving Forces

From retained soil

$$P_s := \left[ \frac{1}{2} \cdot K_a \cdot \gamma_e \cdot (E_n + h'_n)^2 \cdot \cos(\delta_e - \omega) \right] \quad [\text{Eq. 5-6}]$$

$$\boxed{P_s^T = (341 \quad 673 \quad 1205) \cdot \text{plf}}$$

From surcharge

$$P_q := (q_d + q_l) \cdot K_a \cdot (E_n + h'_n) \cdot \cos(\delta_e - \omega) \quad [\text{Eq. 5-8}]$$

$$\boxed{P_q^T = (0 \quad 0 \quad 0) \cdot \text{plf}}$$

### Factor of safety against internal sliding

$$P_a := P_s + P_q \quad [\text{Eq. 5-11}]$$

$$\boxed{P_a^T = (341 \quad 673 \quad 1205) \cdot \text{plf}}$$

$$FS_{sl} := \frac{R'_s + V_{u_n}}{(P_a)} \quad [\text{Eq. 5-48}]$$

$$\boxed{FS_{sl}^T = (6.862 \quad 3.593 \quad 2.376)}$$

## Local Stability of Facing Units

### Facing Connection Strength

$$T_{conn,n} := \min \left[ V_{csmax,n}, a_{cs,n} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs,n}) \right] \quad [\text{Eq. 5-59}]$$

$$T_{conn}^T = (1489 \ 1677 \ 1864) \cdot \text{plf}$$

$$FS_{conn,n} := \frac{T_{conn,n}}{F_{g,n}} \quad FS_{conn}^T = (5.003 \ 5.417 \ 30.28)$$

### Resistance to Bulging

Shear capacity at each geogrid layer

$$V_{u,n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$V_u^T = (1489 \ 1677 \ 1864) \cdot \text{plf}$$

Driving Force at each geogrid layer

$$P_{a,n} := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (E_n)^2 \cdot \cos(\delta_i - \omega) \right] + (q_d + q_l) \cdot K_{a,i} \cdot (E_n) \cdot \cos(\delta_i - \omega) \quad [\text{Eq. 5-11}]$$

$$P_a^T = (184 \ 439 \ 803) \cdot \text{plf}$$

Sum of tension in reinforcement layers above layer being considered

$$F_{n+1} := \sum_{i=1}^n F_{g,i}$$

$$F^T = (0 \ 298 \ 607 \ 669) \cdot \text{plf}$$

$$FS_{sc,n} := \frac{V_{u,n}}{P_{a,n} - F_n} \quad [\text{Eq. 5-61}]$$

$$FS_{sc}^T = (8.101 \ 11.881 \ 9.525)$$

### Maximum unreinforced height of SRW units

$$y := E_1 = 3.67 \text{ ft}$$

$$q_w := 0 \cdot \text{psf}$$

Moment equilibrium

Driving Moments

$$P'_s := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (y)^2 \cdot \cos(\delta_i - \omega) \right] \quad [\text{Eq. 4-5}]$$

$$P'_s = 183.809 \cdot \text{plf}$$

$$P'_q := (q_d + q_l) \cdot K_{a_i} \cdot (y) \cdot \cos(\delta_i - \omega) \quad [\text{Eq. 4-6}]$$

$$P'_q = 0 \cdot \text{plf}$$

$$P'_a := P'_s + P'_q \quad [\text{Eq. 4-4}]$$

$$P'_a = 183.809 \cdot \text{plf}$$

$$Y'_s := \frac{1}{3} \cdot y \quad [\text{Eq. 4-7}]$$

$$Y'_s = 1.223 \text{ ft}$$

$$Y'_q := \frac{1}{2} \cdot y \quad [\text{Eq. 4-8}]$$

$$Y'_q = 1.84 \text{ ft}$$

$$M'_o := P'_s \cdot Y'_s + P'_q \cdot Y'_q \quad [\text{Eq. 4-17}]$$

$$M'_o = 224.86 \cdot \text{lbf}$$

### Resisting Moments

$$W'_w := y \cdot \gamma_u \cdot W_u \quad [\text{Eq. 4-9}]$$

$$W'_w = 440.4 \cdot \text{plf}$$

$$X'_w := G_u + \frac{1}{2} \cdot (y) \cdot \tan(\omega) \quad [\text{Eq. 4-16}]$$

$$X'_w = 0.729 \text{ ft}$$

$$M'_r := W'_w \cdot X'_w \quad [\text{Eq. 4-15}]$$

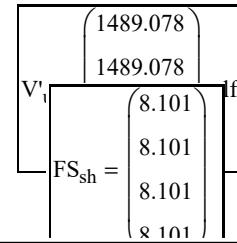
$$M'_r = 321.217 \text{ ft} \cdot \text{plf}$$

$$FS_{ot} := \frac{M'_r}{M'_o} \quad [\text{Eq. 4-14}]$$

$$FS_{ot} = 1.429$$

### Factor of Safety against Shear failure

$$V'_u := a_{cs} + W'_w \cdot \tan(\lambda_{cs}) \quad [\text{Eq. 4-25}]$$



$$FS_{sh} := \frac{V'_u}{P'_a} \quad [\text{Eq. 4-27}]$$

## Summary

Wall Height

$$H = 7 \text{ ft}$$

Unreinforced Stability

$$FS_{ot} = 1.429$$

$$FS_{bearing} = 5.049$$

Applied Bearing Stress

$$Q_a = 863 \cdot \text{psf}$$

Grid Elevation	Geogrid Length	Tensile Force	Geogrid Strength	Anch. Length	Anch. Capacity	FS Grid Tension (1.0)	FS Pullout (1.5)	FS Int Sliding (1.5)	FS Conn (1.5)	FS Bulging (1.5)
$E_n =$	$L_n =$	$\frac{F_{g_n}}{\text{plf}} =$	$\frac{T_{a_n}}{\text{plf}} =$	$L_{a_n} =$	$\frac{AC_n}{\text{plf}} =$	$FS_{ten\_n} =$	$FS_{po\_n} =$	$FS_{sl\_n} =$	$FS_{conn\_n} =$	$FS_{sc\_n} =$
3.67	ft	5	ft	298	834	1.5	570	2.8	1.92	6.86
5.67		5		310	834	2.79	1554	2.69	5.02	3.59
7.67		5		62	834	4.08	2995	13.55	48.66	2.38

# Segmental Retaining Wall Design Calculations per NCMA

## Wall Geometry

Height $H_{\text{av}} := 6.33 \cdot \text{ft}$	Backslope $\beta := 10.0 \cdot \text{deg}$	Dead Load $q_d := 0 \cdot \text{psf}$	Live Load $q_l := 0 \cdot \text{psf}$	Distance to Slope $Z := 1.0 \cdot \text{ft}$	Wall below grade at toe $H_{\text{cmb}} := .67 \cdot \text{ft}$
---	---	--	--	---	--

## Soil Properties

Reinforced Soil (Internal) $\gamma_i := 110 \cdot \text{pcf}$ $\phi_i := 32 \cdot \text{deg}$ $C_{\text{dsi}} := 0.8$	Retained Soil (External) $\gamma_e := 120 \cdot \text{pcf}$ $\phi_e := 26 \cdot \text{deg}$ $C_{\text{dse}} := 1.0$	Drainage Fill $\gamma_d := 110 \cdot \text{pcf}$ $\phi_d := 32 \cdot \text{deg}$	Foundation Soil $\gamma_f := 120 \cdot \text{pcf}$ $\phi_f := 26 \cdot \text{deg}$ $c_f := 0.0 \text{ psf}$	Pullout $C_i := 0.7$
---	---	--	--	-------------------------

## Segmental Unit Properties

Height $H_u := 8 \cdot \text{in}$	Length $L_u := 18 \cdot \text{in}$	Width $W_u := 12 \cdot \text{in}$	Setback $\Delta_u := 1.0 \cdot \text{in}$	Center of Gravity $G_u := 6 \cdot \text{in}$	Batter $\omega := \tan\left(\frac{\Delta_u}{H_u}\right)$ $\omega = 7.125 \cdot \text{deg}$
Infilled Unit Weight $\gamma_u := 120 \cdot \text{pcf}$	Hinge Height $H_h := \text{if} \left[ \tan(\omega) = 0, H, \left[ 2 \cdot \frac{(W_u - G_u)}{\tan(\omega)} \right] \right] \Rightarrow H_h = 8 \text{ ft}$				[Eq. 4-1]

### Internal Interface Friction Angle

$$\delta_i := \frac{2}{3} \cdot \phi_i \quad [\delta_i = 21.33 \cdot \text{deg}] \quad [\text{Eq. 3-17}]$$

### Internal Active Earth Pressure

$$K_{a_i} := \frac{\cos(\phi_i + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_i) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_i + \delta_i) \cdot \sin(\phi_i - \beta)}{\cos(\omega - \delta_i) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{a_i} = 0.256]$$

### External Interface Friction Angle

$$\delta_e := \text{if}(\phi_i > \phi_e, \phi_e, \phi_i) \quad [\delta_e = 26 \cdot \text{deg}] \quad [\text{Eq. 3-16}]$$

### External Active Earth Pressure

$$K_{a_e} := \frac{\cos(\phi_e + \omega)^2}{\cos(\omega)^2 \cdot \cos(\omega - \delta_e) \cdot \left[ 1 + \sqrt{\left( \frac{\sin(\phi_e + \delta_e) \cdot \sin((\phi_e - \beta))}{\cos(\omega - \delta_e) \cdot \cos(\omega + \beta)} \right)^2} \right]^2} \quad [\text{Eq. 3-11}] \quad [K_{a_e} = 0.339]$$

### Orientation of Critical Internal Failure Surface

$$\alpha_i := \text{atan} \left[ \frac{-\tan(\phi_i - \beta) + \sqrt{(\tan(\phi_i - \beta)) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega)) \cdot (1 + \tan(\delta_i - \omega) \cdot \cot(\phi_i + \omega))}}{1 + \tan(\delta_i - \omega) \cdot (\tan(\phi_i - \beta) + \cot(\phi_i + \omega))} \right] + \phi_i \quad [\text{Eq. 3-14}] \quad [\alpha_i = 52.419 \cdot \text{deg}]$$

### Orientation of Critical External Failure Surface

$$\alpha_e := \text{atan} \left[ \frac{-\tan(\phi_e - \beta) + \sqrt{\tan(\phi_e - \beta) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega)) \cdot (1 + \tan(\delta_e - \omega) \cdot \cot(\phi_e + \omega))}}{1 + \tan(\delta_e - \omega) \cdot (\tan(\phi_e - \beta) + \cot(\phi_e + \omega))} \right] + \phi_e \quad [\text{Eq. 3-14}] \quad [\alpha_e = 46.452 \cdot \text{deg}]$$

**Sliding****External Stability Analysis**

Given

$$\min \left[ \frac{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_e)}{1.5} \right]$$

$$\min \left[ \frac{C_{dse} \cdot \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_d)}{1.5} \right]$$

$$1.5 = \frac{C_{dse} \cdot c_f \cdot L + \left[ q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] + L \cdot \gamma_e \cdot H \dots + \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \tan(\phi_f)}{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \dots + (q_d + q_l) \cdot K_a_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]}$$

**Overshooting**

$L_{\text{sliding}} := \text{Find}(L)$

$L_{\text{sliding}} = 3.34 \text{ ft}$

Given

$$2.0 = \frac{\left[ (L \cdot \gamma_e \cdot H) \cdot \left[ \frac{1}{2} \cdot (L + H \cdot \tan(\omega)) \right] \right] \dots + \left[ \frac{1}{2} \cdot \gamma_e \cdot (L - W_u - Z) \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \left[ H \cdot \tan(\omega) + W_u + Z + \frac{2}{3} \cdot (L - W_u - Z) \right] + q_d \cdot \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \frac{Z + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right]}{2} + H \cdot \tan(\omega) +}{\left[ \frac{1}{2} \cdot K_a_e \cdot \gamma_e \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right]^2 \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{3} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right] \cdot \left[ \frac{1}{2} \cdot \left[ H + \left[ (L - W_u - Z) + \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} \right] \cdot \tan(\beta) \right] \cdot \cos(\delta_e - \omega) \right]}$$

$L_{\text{overtaking}} := \text{Find}(L)$

$L_{\text{overtaking}} = 2.631 \text{ ft}$

$$L := \max \begin{pmatrix} L_{\text{sliding}} \\ L_{\text{overtaking}} \\ 0.6 \cdot H \end{pmatrix}$$

$L = 3.798 \text{ ft}$

Based on Overtaking and Sliding:

$L := 5.0 \text{ ft}$

## Eccentricity

$$L' := L - W_u - Z$$

$$L' = 3 \text{ ft}$$

[Fig. 2-10] [Eq. 5-1]

$$L'' := \frac{(L - W_u - Z) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)}$$

$$L'' = 0.068 \text{ ft}$$

[Fig. 2-10] [Eq. 5-2]

$$L_\beta := L' + L''$$

$$L_\beta = 3.068 \text{ ft}$$

[Fig. 2-10] [Eq. 5-3]

$$h := L_\beta \cdot \tan(\beta)$$

$$h = 0.541 \text{ ft}$$

[Fig. 2-10] [Eq. 5-4]

$$W_{ri} := L \cdot \gamma_i \cdot H$$

$$W_{ri} = 3481.5 \cdot \text{plf}$$

[Eq. 5-15]

$$X_{ri} := \frac{1}{2} \cdot (L + H \cdot \tan(\omega))$$

$$X_{ri} = 2.896 \text{ ft}$$

[Eq. 5-19]

$$W_{r\beta} := \frac{1}{2} \cdot \gamma_i \cdot (L' - Z) \cdot h$$

$$W_{r\beta} = 59.499 \cdot \text{plf}$$

[Eq. 5-16]

$$X_{r\beta} := H \cdot \tan(\omega) + W_u + \frac{2}{3} \cdot L_\beta + Z$$

$$X_{r\beta} = 4.836 \text{ ft}$$

[Eq. 5-20]

$$X_{q\beta} := \frac{Z + L_\beta}{2} + [(H + h) \cdot \tan(\omega)] + W_u$$

$$X_{q\beta} = 3.893 \text{ ft}$$

[Eq. 5-21]

Actual Height of wall:

$$H_s := (H + h)$$

$$H_s = 6.871 \text{ ft}$$

Earth Pressures:

$$P_{sH} := \left[ \frac{1}{2} \cdot K_a e \cdot \gamma_e \cdot (H + h)^2 \cdot \cos(\delta_e - \omega) \right]$$

$$P_{sH} = 908.721 \cdot \text{plf}$$

[Eq. 5-6]

$$Y_s := \frac{1}{3} \cdot (H + h)$$

$$Y_s = 2.29 \text{ ft}$$

[Eq. 5-9]

$$P_{qH} := (q_d + q_l) \cdot K_a e \cdot (H + h) \cdot \cos(\delta_e - \omega)$$

$$P_{qH} = 0 \cdot \text{plf}$$

[Eq. 5-8]

$$Y_q := \frac{1}{2} \cdot (H + h)$$

$$Y_q = 3.435 \text{ ft}$$

[Eq. 5-10]

$$\frac{e := \left[ P_{sH} \cdot Y_s + P_{qH} \cdot Y_q - W_{ri} \cdot \left( X_{ri} - \frac{L}{2} \right) - W_{r\beta} \cdot \left( X_{r\beta} - \frac{L}{2} \right) - q_d \cdot (L_\beta) \cdot \left( X_{q\beta} - \frac{L}{2} \right) \right]}{W_{ri} + W_{r\beta} + q_d \cdot (L_\beta)}$$

$$e = 0.1595 \text{ ft}$$

[Eq. 5-25]

Check  $\textcolor{green}{e} := \text{if}(e \leq 0, 0.075L, e)$

$$e = 0.16 \text{ ft}$$

Surcharge is applied over:

$$(L' + L'') = 3.068 \text{ ft}$$

$$B := L - 2 \cdot e$$

$$B = 4.681 \text{ ft}$$

[Eq. 5-24]

## Bearing Capacity

$$Q_a := \frac{[W_{ri} + W_{rf\beta} + (q_d + q_l) \cdot (L' + L'')]}{B}$$

$$Q_a = 756.469 \cdot \text{psf}$$

$$N_q := \tan\left(45^\circ - \frac{\phi_f}{2}\right)^2 \cdot \exp(\pi \cdot \tan(\phi_f))$$

$$N_q = 11.854$$

[Fig. 4-5]

$$N_c := \text{if } [\phi_f = 0, 5.14, (N_q - 1) \cdot \cot(\phi_f)]$$

$$N_c = 22.254$$

[Fig. 4-5]

$$N_\gamma := 2 \cdot (N_q + 1) \cdot \tan(\phi_f)$$

$$N_\gamma = 12.539$$

[Fig. 4-5]

$$Q_{ult} := c_f \cdot N_c + \frac{1}{2} \cdot \gamma_f \cdot B \cdot N_\gamma + \gamma_f \cdot H_{emb} \cdot N_q$$

$$Q_{ult} = 4474.7 \cdot \text{psf}$$

[Eq. 4-20]

$$FS_{bearing} := \frac{Q_{ult}}{Q_a}$$

$$FS_{bearing} = 5.915$$

[Eq. 4-19]

## Internal Stability

### Reinforcement Properties

#### Geogrid Design Data

Backfill Soil      Type := (gravel)

1    2    3    4    5    6    7    8    9

Geogrid Number

$$\text{Type}^T = (411 \ 834 \ 1199 \ 1336 \ 2004 \ 2508 \ 3011 \ 3873 \ 7914)$$

$$GN1 := 4$$

$$GN2 := 2$$

$$\text{inter}^T = (1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 1145 \ 0)$$

$$\text{slope}^T = (38 \ 38 \ 38 \ 38 \ 38 \ 38 \ 0)$$

$$\text{maxc}^T = (4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 4540 \ 0) \quad x := 4..1 \quad x \text{ is the number of grids at the top of the wall of a different type}$$

$$T_a := \text{Type}_{GN1} \cdot \text{plf} \quad T_a = 1336 \cdot \text{plf}$$

$$T_{a2} := \text{Type}_{GN2} \cdot \text{plf} \quad T_{a2} = 834 \cdot \text{plf}$$

$$a_{cs} := \text{inter}_{GN1} \cdot \text{plf} \quad a_{cs} = 1145 \cdot \text{plf}$$

$$\lambda_{cs} := \text{slope}_{GN1} \cdot \text{deg} \quad \lambda_{cs} = 38 \cdot \text{deg}$$

$$V_{csmax} := \text{maxc}_{GN1} \cdot \text{plf} \quad V_{csmax} = 4540 \cdot \text{plf}$$

$$a_{cs2} := \text{inter}_{GN2} \cdot \text{plf} \quad a_{cs2} = 1145 \cdot \text{plf}$$

$$\lambda_{cs2} := \text{slope}_{GN2} \cdot \text{deg} \quad \lambda_{cs2} = 38 \cdot \text{deg}$$

$$V_{csmax2} := \text{maxc}_{GN2} \cdot \text{plf} \quad V_{csmax2} = 4540 \cdot \text{plf}$$

## Tension in Geogrid

Number of Grids:	Grig Spacing (ft):	# of grids for that spacing:	Depth of first grid (ft):	Length of grids:
$n_g := 2$	Spacing1 := 2	$n_1 := 2$	$h_1 := 3.67$	$L_1 := 5.0 \quad L_2 := 5.0 \quad L_t := \frac{L}{\text{ft}}$
	Spacing2 := 1.67	$n_2 := 0$		

Make all zero when using one geogrid

Note: make sure that the elevations don't exceed the height of the wall (H)  $H = 6.33 \text{ ft}$

$$\begin{aligned} \text{top} &:= \text{length}(E) & p &:= 2 \dots \text{top} & \text{top} &= 2 \\ \text{grids} &:= \text{length}(E) & n &:= 1 \dots \text{top} & l &:= 1 \dots \text{grids} - 1 \end{aligned}$$

$$\begin{aligned} E &= \begin{pmatrix} 3.67 \\ 5.67 \end{pmatrix} \text{ ft} & T_a &:= \frac{\overrightarrow{L \cdot T_a}}{L} & L &= \begin{pmatrix} 5 \\ 5 \end{pmatrix} \text{ ft} \\ T_{a_x} &:= T_{a2} & T_{a_x} &= \begin{pmatrix} 834 \\ 834 \\ 834 \\ 834 \end{pmatrix} \cdot \text{plf} & T_a &= \begin{pmatrix} 1336 \\ 1336 \end{pmatrix} \cdot \text{plf} \end{aligned}$$

$$T_a^T = (834 \ 834 \ 834 \ 834) \cdot \text{plf}$$

$$D_p := \frac{E_{p-1} + E_p}{2} \quad D_1 := 0 \cdot \text{ft} \quad D_{\text{grids}+1} := H$$

$$D^T = (0 \ 4.67 \ 6.33) \text{ ft}$$

### Total Applied Tensile Strength in the Geosynthetic reinf.:

$$F_{g_n} := \int_{D_n}^{D_{(n+1)}} (\gamma_i \cdot D + q_l + q_d) \cdot K a_i \cdot \cos(\delta_i - \omega) \, dD \quad [\text{Eq. 5-36}]$$

$$F_g^T = (297.624 \ 249.193) \cdot \text{plf}$$

### Safety factor:

$$FS_{ten_n} := \frac{T_{a_n}}{F_{g_n}} \quad FS_{ten}^T = (2.802 \ 3.347)$$

## Pullout Capacity

### Anchorage Length of Geosynthetic

$$La_n := L_n - W_u - [(H + h) - E_n] \cdot \tan(90^\circ - \alpha_i) + [(H + h) - E_n] \cdot \tan(\omega) \quad [\text{Eq. 5-46}]$$

$$La^T = (1.937 \quad 3.226) \text{ ft}$$

**Note:** If the anchorage length is less than 1ft then there is not enough embedment length and it has to be increased. Note that in some cases it might just be the top two grids.

### Average Depth of overburden on Anchorage length

$$d_n := E_n + \left[ (H - E_n) \cdot \tan(90^\circ - \alpha_i) + \frac{La_n}{2} - (Z + H \cdot \tan(\omega) - \Delta_u) \right] \cdot \tan(\beta) \quad [\text{Eq. 5-47}]$$

$$d^T = (3.901 \quad 5.743) \text{ ft}$$

### Anchorage Capacity

$$AC_n := 2 \cdot La_n \cdot C_i \cdot (d_n \cdot \gamma_i + q_d) \cdot \tan(\phi_i) \quad [\text{Eq. 5-45}]$$

$$AC^T = (726.96 \quad 1782.741) \cdot \text{plf}$$

$$F_g^T = (297.624 \quad 249.193) \cdot \text{plf}$$

### Safety Factor

$$FS_{po} := \frac{\overrightarrow{AC}}{F_g} \quad [\text{Eq. 5-44}]$$

$$FS_{po}^T = (2.443 \quad 7.154)$$

## Internal Sliding

### Reduced reinforcement length

$$\Delta L_{l+1} := \begin{cases} \left[ (E_{l+1} - E_l) \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) \right] & \text{if } n_g > 2 \\ \text{Spacing} \cdot 1 \cdot \text{ft} \cdot \left( \frac{1}{\tan(\alpha_e)} - \tan(\omega) \right) & \text{if } n_g = 2 \\ 0 & \text{if } n_g = 1 \end{cases} \quad [\text{Eq. 5-51}]$$

$$\Delta L^T = (0 \quad 1.651) \text{ ft}$$

$$L'_{s_n} := L_n - W_u - \Delta L_n \quad [\text{Eq. 5-50}]$$

$$L'_s^T = (4 \quad 2.349) \text{ ft}$$

### Length of sloping ground

$$L_{s\beta_n} := L'_{s_n} + \frac{(L'_{s_n} - W_u) \cdot \tan(\beta) \cdot \tan(\omega)}{1 - \tan(\beta) \cdot \tan(\omega)} - Z \quad [\text{Eq. 5-53 & 5-52}]$$

$$\boxed{L_{s\beta}^T = (3.068 \quad 1.379) \text{ ft}}$$

### Height of slope above crest of wall

$$h'_n := L_{s\beta_n} \cdot \tan(\beta) \quad [\text{Eq. 5-54}]$$

$$\boxed{h^T = (0.541 \quad 0.243) \text{ ft}}$$

### Weight of reduced reinforced area

$$W'_{ri_n} := L'_{s_n} \cdot E_n \cdot \gamma_i \quad [\text{Eq. 5-55}]$$

$$\boxed{W'_{ri}^T = (1615 \quad 1465) \cdot \text{plf}}$$

### Weight of wedge beyond reinforced soil zone

$$W'_{r\beta_n} := \frac{1}{2} \cdot \left( L_{s\beta_n} \cdot h'_n \right) \cdot \gamma_i \quad [\text{Eq. 5-56}]$$

$$\boxed{W'_{r\beta}^T = (91.26 \quad 18.45) \cdot \text{plf}}$$

### Friction developed by weight

$$R'_{s_n} := C_{dsi} \cdot \left[ q_d \cdot \left( L_{s\beta_n} + Z \right) + W'_{ri_n} + W'_{r\beta_n} \right] \cdot \tan(\phi_i) \quad [\text{Eq. 5-49}]$$

$$\boxed{R'_s^T = (853 \quad 742) \cdot \text{plf}}$$

### Shear capacity of facing elements

$$V_{u_n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$\boxed{V_u^T = (1489 \quad 1677) \cdot \text{plf}}$$

### Driving Forces

From retained soil

$$P_{s_n} := \left[ \frac{1}{2} \cdot K_a e \cdot \gamma_e \cdot (E_n + h'_n)^2 \cdot \cos(\delta_e - \omega) \right] \quad [\text{Eq. 5-6}]$$

$$\boxed{P_s^T = (341 \quad 673) \cdot \text{plf}}$$

From surcharge

$$P_{q_n} := (q_d + q_l) \cdot K_a e \cdot (E_n + h'_n) \cdot \cos(\delta_e - \omega) \quad [\text{Eq. 5-8}]$$

$$\boxed{P_q^T = (0 \quad 0) \cdot \text{plf}}$$

### Factor of safety against internal sliding

$$P_{a_n} := P_{s_n} + P_{q_n} \quad [\text{Eq. 5-11}]$$

$$\boxed{P_a^T = (341 \quad 673) \cdot \text{plf}}$$

$$FS_{sl_n} := \frac{R'_{s_n} + V_{u_n}}{(P_{a_n})} \quad [\text{Eq. 5-48}]$$

$$\boxed{FS_{sl}^T = (6.862 \quad 3.593)}$$

## Local Stability of Facing Units

### Facing Connection Strength

$$T_{conn,n} := \min \left[ V_{csmax,n}, a_{cs,n} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs,n}) \right] \quad [\text{Eq. 5-59}]$$

$$\boxed{T_{conn}^T = (1489 \quad 1677) \cdot \text{plf}}$$

$$FS_{conn,n} := \frac{T_{conn,n}}{F_{g,n}} \quad \boxed{FS_{conn}^T = (5.003 \quad 6.728)}$$

### Resistance to Bulging

Shear capacity at each geogrid layer

$$V_{u,n} := \min \left[ V_{csmax}, a_{cs} + \left( \text{if}(E_n > H_h, H_h, E_n) \cdot \gamma_u \cdot W_u \right) \cdot \tan(\lambda_{cs}) \right] \quad [\text{Eq. 4-25}]$$

$$\boxed{V_u^T = (1489 \quad 1677) \cdot \text{plf}}$$

Driving Force at each geogrid layer

$$P_{a,n} := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (E_n)^2 \cdot \cos(\delta_i - \omega) \right] + (q_d + q_l) \cdot K_{a,i} \cdot (E_n) \cdot \cos(\delta_i - \omega) \quad [\text{Eq. 5-11}]$$

$$\boxed{P_a^T = (184 \quad 439) \cdot \text{plf}}$$

Sum of tension in reinforcement layers above layer being considered

$$F_{n+1} := \sum_{i=1}^n F_{g,i}$$

$$\boxed{F^T = (0 \quad 298 \quad 547) \cdot \text{plf}}$$

$$FS_{sc,n} := \frac{V_{u,n}}{P_{a,n} - F_n} \quad [\text{Eq. 5-61}]$$

$$\boxed{FS_{sc}^T = (8.101 \quad 11.881)}$$

### Maximum unreinforced height of SRW units

$$y := E_1 = 3.67 \text{ ft}$$

$$\gamma_w := 0 \text{ psf}$$

Moment equilibrium

Driving Moments

$$P'_s := \left[ \frac{1}{2} \cdot K_{a,i} \cdot \gamma_i \cdot (y)^2 \cdot \cos(\delta_i - \omega) \right] \quad [\text{Eq. 4-5}]$$

$$\boxed{P'_s = 183.809 \cdot \text{plf}}$$

$$P'_q := (q_d + q_l) \cdot K_{a_i} \cdot (y) \cdot \cos(\delta_i - \omega)$$

[Eq. 4-6]

$$P'_q = 0 \cdot \text{plf}$$

$$P'_a := P'_s + P'_q$$

[Eq. 4-4]

$$P'_a = 183.809 \cdot \text{plf}$$

$$Y'_s := \frac{1}{3} \cdot y$$

[Eq. 4-7]

$$Y'_s = 1.223 \text{ ft}$$

$$Y'_q := \frac{1}{2} \cdot y$$

[Eq. 4-8]

$$Y'_q = 1.84 \text{ ft}$$

$$M'_o := P'_s \cdot Y'_s + P'_q \cdot Y'_q$$

[Eq. 4-17]

$$M'_o = 224.86 \cdot \text{lbf}$$

### Resisting Moments

$$W'_w := y \cdot \gamma_u \cdot W_u$$

[Eq. 4-9]

$$W'_w = 440.4 \cdot \text{plf}$$

$$X'_w := G_u + \frac{1}{2} \cdot (y) \cdot \tan(\omega)$$

[Eq. 4-16]

$$X'_w = 0.729 \text{ ft}$$

$$M'_r := W'_w \cdot X'_w$$

[Eq. 4-15]

$$M'_r = 321.217 \text{ ft} \cdot \text{plf}$$

$$FS_{ot} := \frac{M'_r}{M'_o}$$

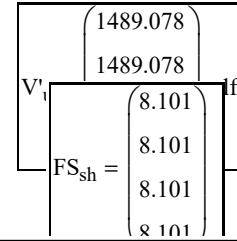
[Eq. 4-14]

$$FS_{ot} = 1.429$$

### Factor of Safety against Shear failure

$$V'_u := a_{cs} + W'_w \cdot \tan(\lambda_{cs})$$

[Eq. 4-25]



$$FS_{sh} := \frac{V'_u}{P'_a}$$

[Eq. 4-27]

## Summary

Wall Height

$$H = 6.33 \text{ ft}$$

Unreinforced Stability

$$FS_{ot} = 1.429$$

$$FS_{bearing} = 5.915$$

Applied Bearing Stress

$$Q_a = 756 \cdot \text{psf}$$

Grid Elevation	Geogrid Length	Tensile Force	Geogrid Strength	Anch. Length	Anch. Capacity	FS Grid Tension (1.0)	FS Pullout (1.5)	FS Int Sliding (1.5)	FS Conn (1.5)	FS Bulging (1.5)
$E_n =$	$L_n =$	$\frac{F_{g_n}}{\text{plf}} =$	$\frac{T_{a_n}}{\text{plf}} =$	$L_{a_n} =$	$\frac{AC_n}{\text{plf}} =$	$FS_{ten\_n} =$	$FS_{po\_n} =$	$FS_{sl\_n} =$	$FS_{conn\_n} =$	$FS_{sc\_n} =$
3.67	5 ft	298	834	1.94 ft	727	2.8	2.44	6.86	5	8.1
5.67	5	249	834	3.23	1783	3.35	7.15	3.59	6.73	11.88